

Fourth Semester B.E. Degree Examination, June-July 2009
Control Systems

Time: 3 hrs.

Max. Marks:100

Note:1. Answer any FIVE full questions, choosing at least two questions from each.
2. Missing data may be suitably assumed.

Part-A

- 1 a. Mention the merits and demerits of open loop and closed loop control systems and give an example for each. (06 Marks)
- b. For the mechanical system shown in figure Q1 (b), obtain the force-voltage analogous network. (08 Marks)

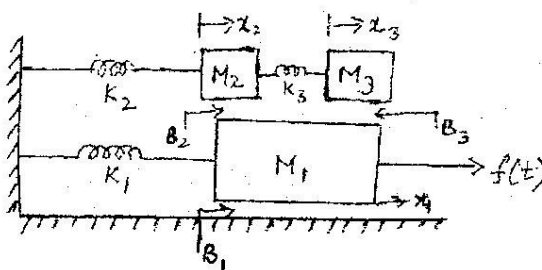


Fig. Q1 (b)

- c. Obtain the transfer function of an armature controlled dc servomotor. (06 Marks)
- 2 a. Explain briefly the following terms:
 - i) Forward path. ii) Path gain. iii) Loop gain. iv) Canonical form. (08 Marks)
 - b. Obtain the C/R ratio for the block diagram shown using block-diagram reduction technique. (06 Marks)

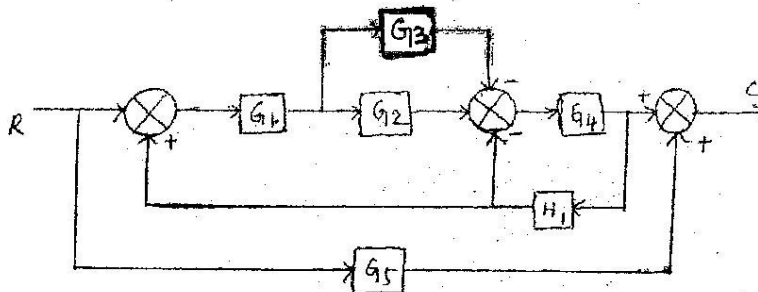


Fig. Q2 (b)

- c. Find $\frac{C(s)}{R(s)}$ by Mason's gain formula (Fig. Q2 (c)). (06 Marks)

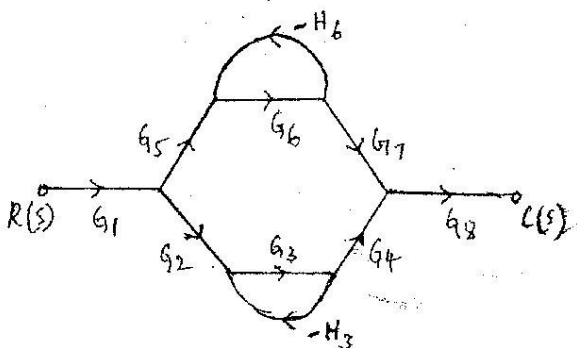


Fig. Q2 (c)

- 3 a. Derive an expression for the under damped response of a second order feed back control system for step input. (06 Marks)
- b. Obtain expressions for rise-time and peak-time for a second-order feed back system response for a step input (under-damped case). (06 Marks)
- c. A positional servomechanism is characterized by an open loop transfer function
- $$G(s) = \frac{k}{s(s+\alpha)}$$
- where k and α are positive constants, for a unity feedback. Find the values of k and α for a damping coefficient value of 0.6 and damped frequency of 8 rad/sec. Also find the peak value of the response when the system is excited by a step of 2 volts. (08 Marks)

- 4 a. Find K_p , K_v and K_a for the system whose open loop transfer function is given by,

$$G(s)H(s) = \frac{10(s+2)(s+3)}{s(s+1)(s+5)(s+4)}$$

Also find the steady-state error for an input $r(t) = 3 + t + t^2$. (08 Marks)

- b. Explain Routh-Hurwitz 's' criterion for determining the stability of a system and mention its limitations. (04 Marks)
- c. A unity feedback control system has:

$$G(s) = \frac{k(s+13)}{s(s+3)(s+7)}$$

Using the Routh's criterion, calculate the range of 'k' for which the system is

- i) Stable
ii) Has its closed loop poles more negative than -1 . (08 Marks)

Part-B

- 5 a. Explain briefly the following terms with respect to root-locus technique:
i) Centroid.
ii) Asymptote.
iii) Break away point. (06 Marks)
- b. Sketch the root locus plot for a closed loop system having an open-loop transfer function:
- $$G(s)H(s) = \frac{k(s+2)}{s(s+1)}$$
- for all values of k from 0 to ∞ . Comment on the stability of the system. (08 Marks)
- c. Show that a part of the root-locus for the open loop transfer function:
- $$G(s)H(s) = \frac{k(s+2)}{s(s+1)}$$
- is a circle. (06 Marks)

- 6 a. The open loop transfer function of a negative feedback control system is:

$$GH(s) = \frac{1}{s(s+1)(s+\frac{1}{2})}$$

Sketch the polar plot and hence find the following:

- i) Phase cross-over frequency.
ii) Gain cross-over frequency.
iii) Gain-margin.
iv) Phase-margin. (10 Marks)
- b. Explain in detail the procedural steps of Nyquist stability criterion. (04 Marks)
- c. A feed back control system has loop transfer function: $GH(s) = \frac{1}{s(s+1)}$. Sketch the Nyquist plot and comment on the stability of a system. (06 Marks)

- 7 a. Derive expressions for resonant peak and resonant frequency for a second order system. (06 Marks)
- b. Find the open-loop transfer function for a unity feed back second order control system for which resonant peak is 1.1 units and resonant frequency is 11.2 radians/sec. (06 Marks)
- c. Sketch the Bode-plot for the transfer function: $G(s) = \frac{Ks^2}{(1+0.2s)(1+0.02s)}$
Determine the value of 'k' for the gain cross over frequency to be 5 rad/sec. (08 Marks)
- 8 a. Compare transfer function approach and state variable approach of analyzing control system. (04 Marks)
- b. A feed back system is characterized by the closed loop transfer function:
$$GH(s) = \frac{s^2 + 3s + 3}{s^3 + 2s^2 + 3s + 1}$$

Obtain its state model. (08 Marks)
- c. State the properties of state transition matrix. Obtain the state transition matrix for:
$$A = \begin{bmatrix} 0 & -1 \\ 2 & -3 \end{bmatrix}$$
 (08 Marks)

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